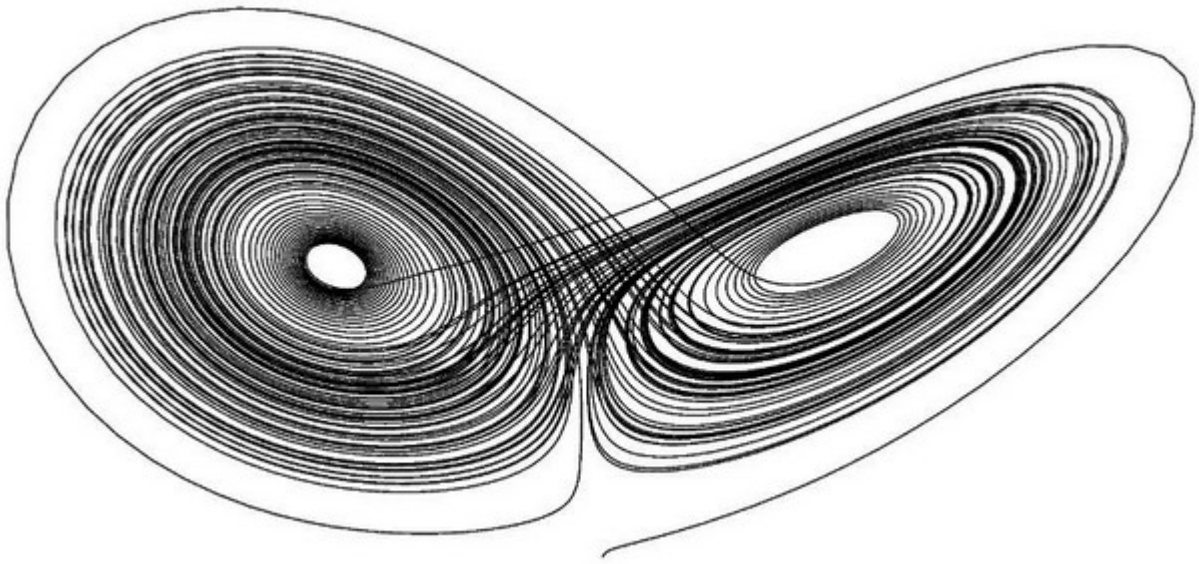
BENESCO Lecture Series on
Sleep, Epilepsy, Consciousness
and Cognition
Bern, Nov. 24th 2017

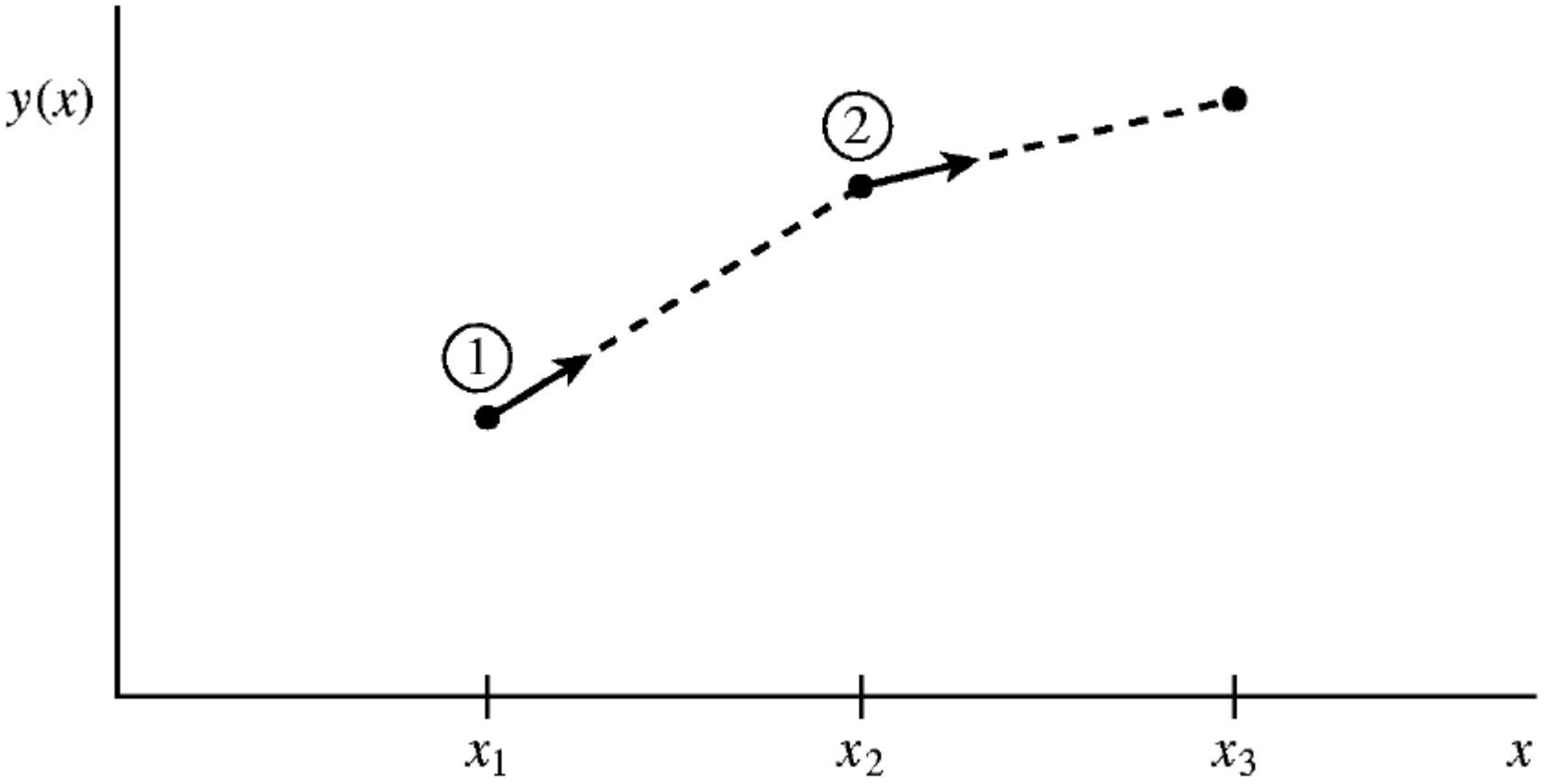
Simple differential equations - introduction using Matlab



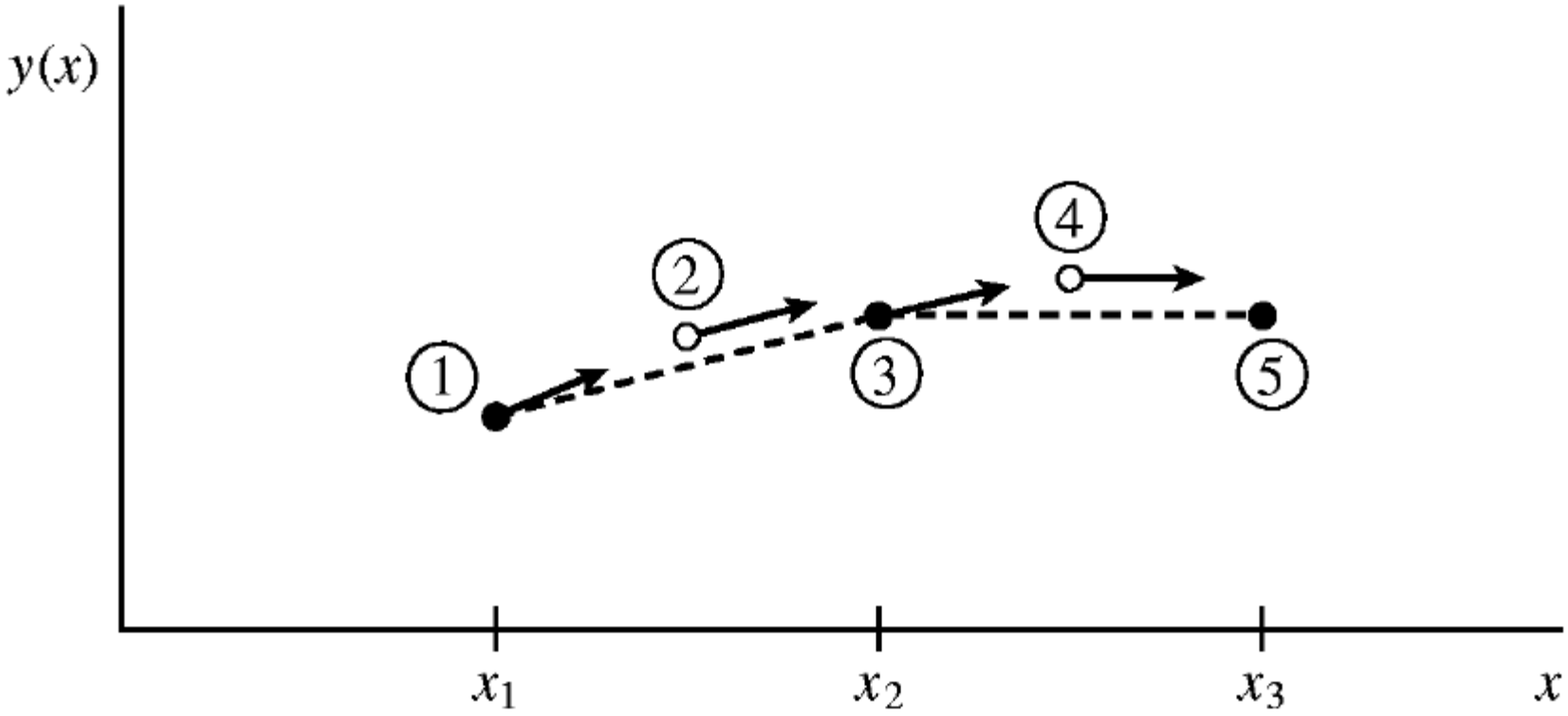
INSELSPITAL
UNIVERSITÄTSSPITAL BERN
HOPITAL UNIVERSITAIRE DE BERNE
BERN UNIVERSITY HOSPITAL

Christian Rummel
SCAN, University Institute of Diagnostic and Interventional Neuroradiology
University of Bern, Inselspital
christian.rummel@insel.ch

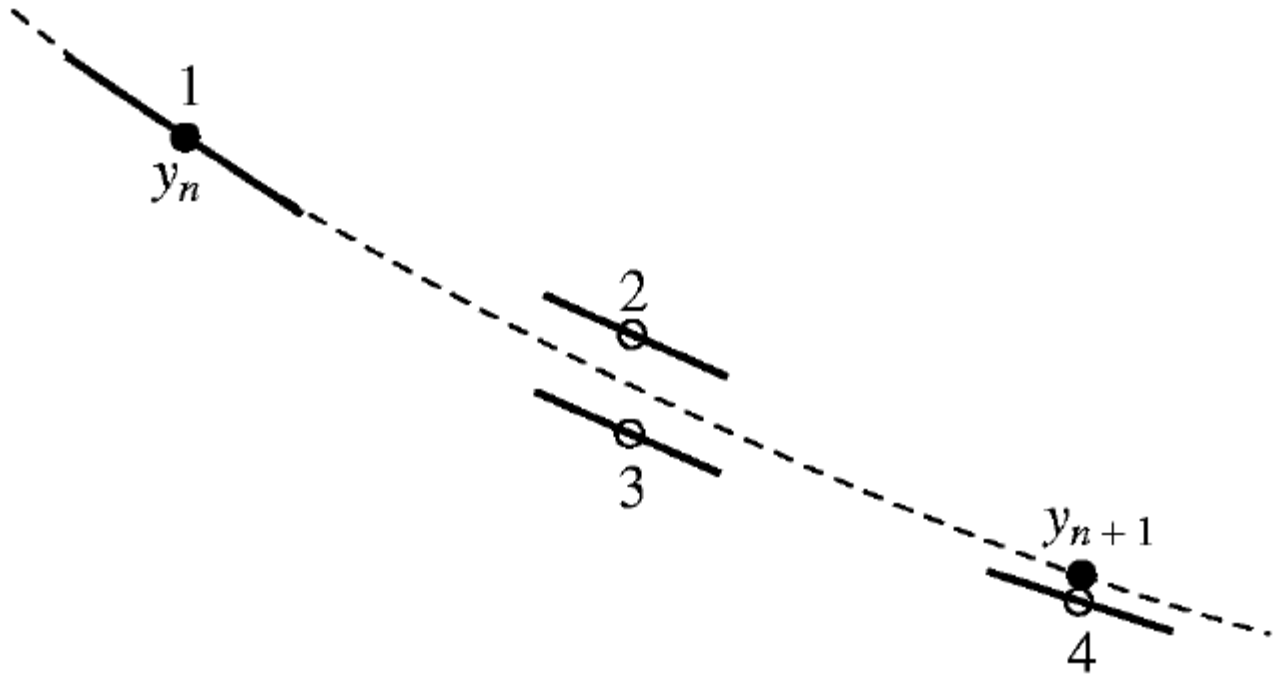
Euler Algorithm (1768–70)



2nd Order Runge-Kutta Algorithm (~1900)

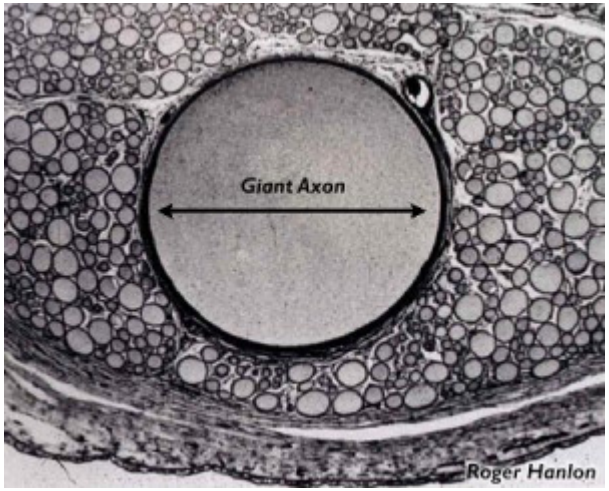


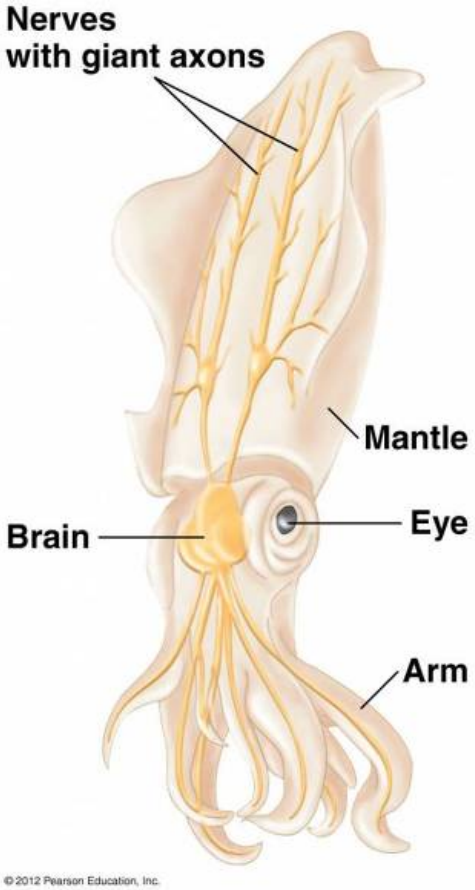
4th Order Runge-Kutta Algorithm (~1900)



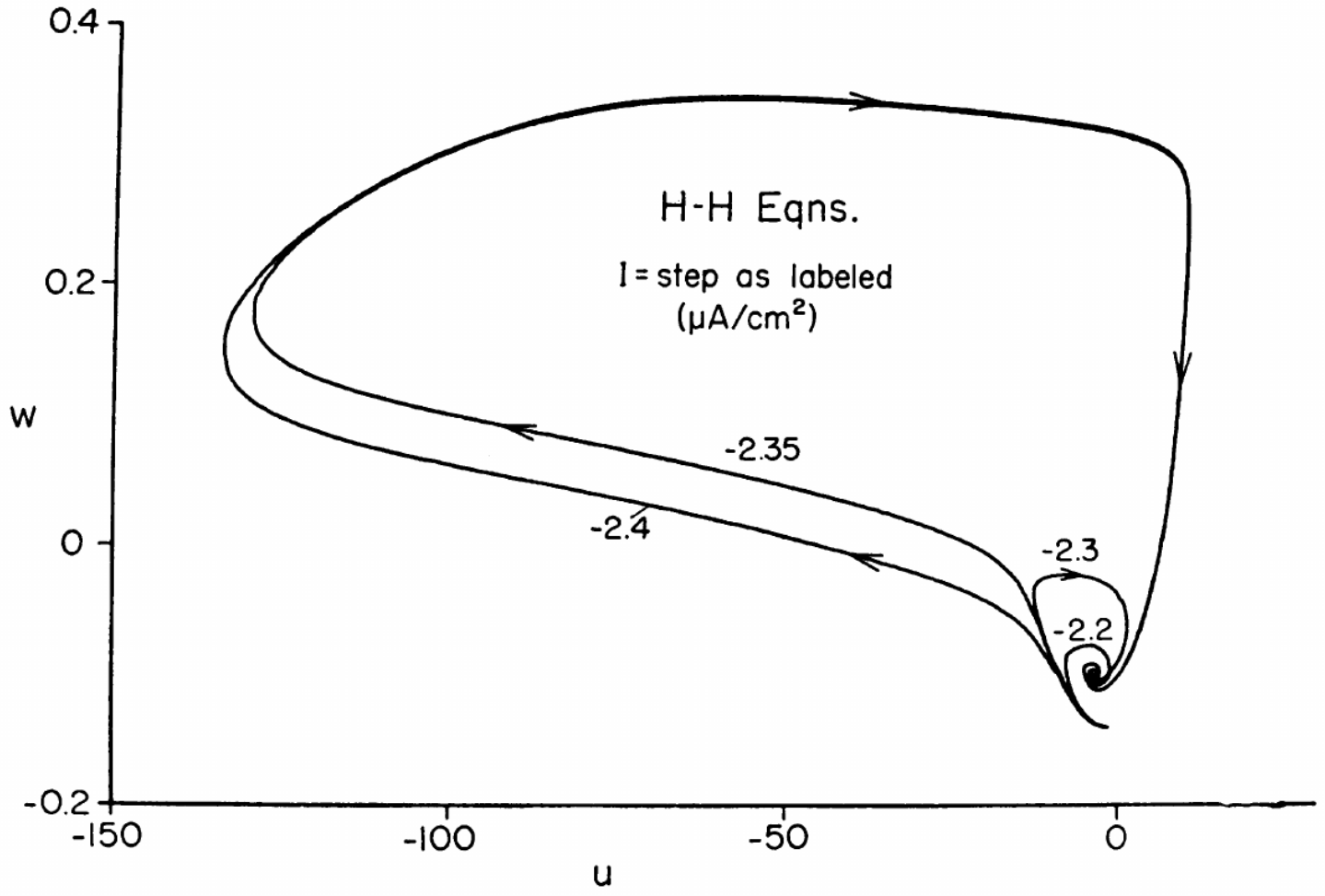
Hodgkin-Huxley Model (1952)

Hodgkin-Huxley Model (1952)



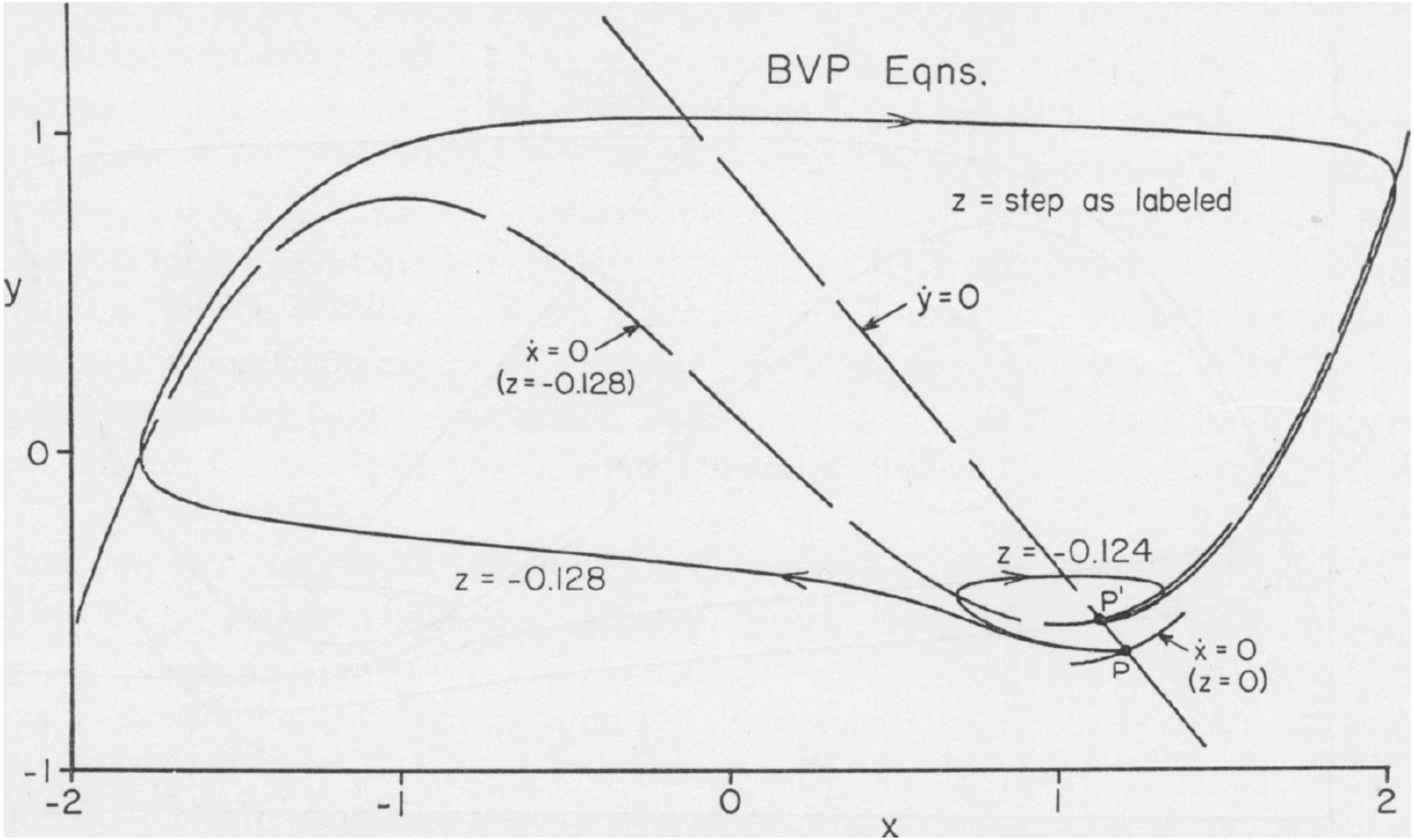


Hodgkin-Huxley Model (1952)



FitzHugh, Biophys J 1 (1961)

FitzHugh-Nagumo Model (1961, 1962)



FitzHugh, Biophys J 1 (1961)

FitzHugh-Nagumo Model (1961, 1962)

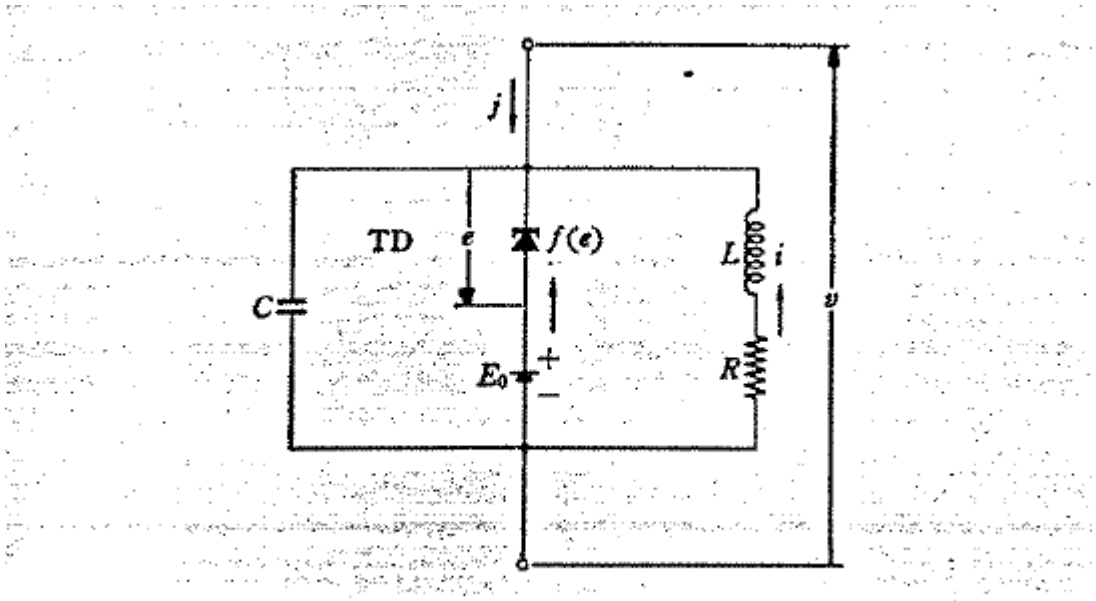


Fig. 2—An electronic simulator of the BVP model.

Nagumo et al., Proc IRE 50 (1962)

Literature

W.H. Press, S.A. Teukolsky, W.T. Vetterling, B.P. Flannery:
Numerical Recipes in C – The Art of Scientific Computing,
2nd edition, Cambridge University Press, 1992

http://lpsa.swarthmore.edu/NumInt/NumIntIntro.html

http://www4.ncsu.edu/~msolufse/LectureFitzHughNagumo.pdf

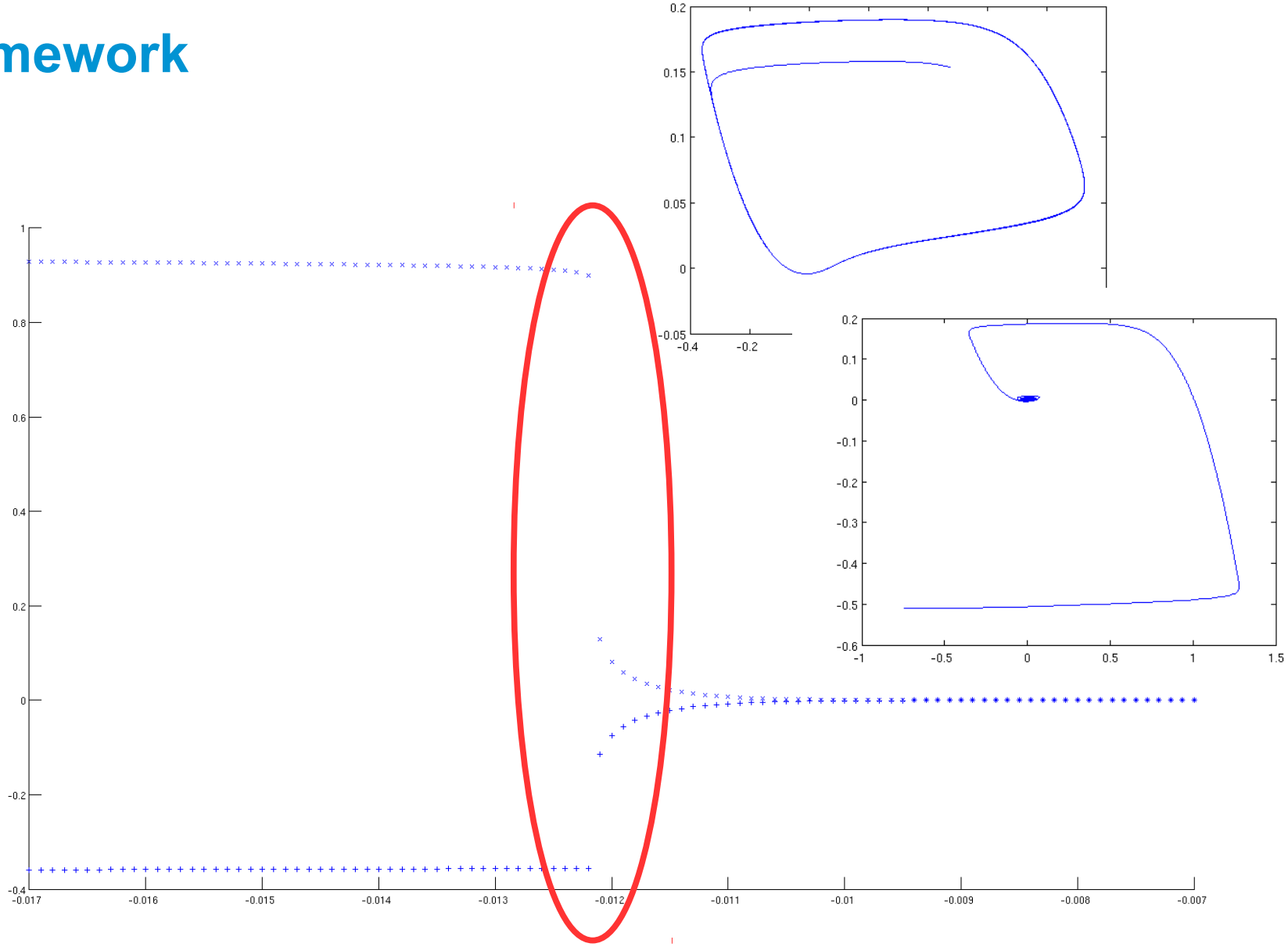
Homework

Appearance of a stable limit cycle in the FitzHugh-Nagumo model ("Hopf bifurcation"):

show numerically that the critical point is $\alpha_0 = -\varepsilon \cdot \gamma$

- write a small Matlab script to ramp up the parameter α of the FitzHugh-Nagumo model ($\varepsilon = 0.008$, $\gamma = 1.5$, $v_{eq} = 0$)
- integrate the differential equation numerically and neglect the transient (be wasteful here!)
- plot the extrema of the v coordinate
- plot example trajectories below and above the bifurcation

Homework


0.2
0.15
0.1
0.05
0
-0.05
-0.4
-0.2
0.2
0.1
0
-0.1
-0.2
-0.3
-0.4
-0.5
-0.6
-1
-0.5
0
0.5
1
1.5
1
0.8
0.6
0.4
0.2
0
-0.2
-0.4
-0.017
-0.016
-0.015
-0.014
-0.013
-0.012
-0.011
-0.01
-0.009
-0.008
-0.007